## A Level Maths

## ( $1^{\text {st }}$ Year Doubles)



Name

## A Level Maths: The Final Countdown

The plan for the rest of the course is shown below: Fill in your topic for each lesson

| Week <br> beginning | Assignment <br> due/ Papers* | Monday <br> Past paper | Wednesday <br> Exam prep | Friday <br> Exam prep |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{2}^{\text {nd }}$ March | Assignment 20 |  |  |  |
| $\mathbf{9}^{\text {th }}$ March | Assignment 21 |  |  |  |
| $\mathbf{1 6}^{\text {th }}$ March | Past paper <br> schedule on <br> Assignment 22 <br> Mock exam in <br> Hall 10am |  |  |  |
| $\mathbf{2 3}^{\text {rd }}$ March |  |  |  |  |
| $\mathbf{3 0}^{\text {th }}$ March |  |  |  |  |
| $\mathbf{2 0}^{\text {th }}$ April |  |  |  |  |
| $\mathbf{2 7}^{\text {th }}$ April |  |  |  |  |
| $\mathbf{4}^{\text {th }}$ May |  |  |  |  |

Study leave starts on Thursday May $7^{\text {th }}$. You should carry on completing the papers during Study Leave. Write them here
11 ${ }^{\text {th }}$ May: $\quad 18^{\text {th }}$ May: $\quad$ 25 $^{\text {th }}$ May:
$\mathbf{1}^{\text {st }}$ June: $\quad \mathbf{8}^{\text {th }}$ June:
*OSC=Old Specification Core Papers (4 hours) P=Pure Paper A=Applied paper
Wednesday will continue to be the day to hand in Assignments/Papers.

## P1 Proof

P2. Algebra and Functions
P3. Coordinate Geometry
P4. Sequences and Series
P5. Trigonometry
P6. Exponentials and Logarithms
P7. Differentiation
P8. Integration
P9. Numerical Methods
P10. Vectors

S1. Sampling
S2. Data Presentation and Interpretation
S3. Probability
S4. Distributions
S5. Hypothesis Testing

M1. Units
M2. Kinematics
M3. Forces
M4. Moments

See pages on jazzymaths for:
Large data set practice
Proofs you need to know The exam specifications

The key to success is honest self-assessment followed by remedial action. If you are honest with yourself about how much you understand the work and if you take remedial action to improve your weak areas, you will get a grade A* (unless you make lots of expensive errors).

## The Mark Scheme is Your Enemy

When you work through these papers, do NOT use the mark scheme every time you get stuck. Try to work out what to do yourself. You won't have the mark scheme in the real exam! Do the test in 2 hours and then mark it. If you don't get full marks on a question, find out what went wrong (use your Survival Kit or the textbook or any other form of support). Then go back to it a day later and do it again (without looking at the mark scheme). Keep doing this until you can get the question right without help. This is the way you will improve your understanding.

In the mark schemes, the following symbols are used:
M marks: method marks are awarded for 'knowing a method and attempting to apply it'.
A marks: Accuracy marks can only be awarded if the relevant method ( $M$ ) marks have been earned.
B marks are for the correct answer (method not necessary)

## Support

If you get stuck there are a number of things you can do

- Refer to your Survival Kit
- Watch the videos again
- Use the textbook and read the bits between the exercises
- Try some of the questions in the exercises to get further help
- Drop In With The Doubles in room 7
- Look at videos and resources from other websites

However, the best thing you can do is figure it out yourself.

## Formulae to Learn

Make sure you remember all the formulae (see later in this booklet)
The formulae that you don't need to remember are in the formula book (also see later in this booklet)

## DO NOT simply copy out the mark scheme.

Here is why you must study the exam papers. By following this programme of exam paper study, you will:
Improve your knowledge of how to solve standard problems. By completing every question from past papers and practice papers you will encounter almost every question that has been put into your real exam.

Improve the accuracy of your algebra... The exam board have told us that the only difference between E grade students and A grade students is that the A grade students make fewer algebraic errors. Being able to answer the questions is not enough. You need to be able to answer them without making expensive errors, and this is not something you can learn at the last minute. It takes practice.

Improve the speed of your algebra... Your real exam will be an algebra sprint. It is very important that you get used to the speed required.

## Studying an exam paper is not the same as doing an exam paper.

## This what you should not do:

Sit down and complete an exam paper.....
After an hour you have done all you can do so you mark your work using the mark scheme.

You realise you've made some errors and you think 'oops! - I won't do that in the exam!'
You read the solutions to the questions you couldn't do and think 'oh - I see how to do it now'.

What has this process done to improve your chance of getting a good grade in the real exam?

Do you have any more knowledge? NO. You have read the solutions to the questions you couldn't do, but this doesn't mean you can actually do them.

Have you improved the accuracy of your algebra? NO. As soon as you finished the paper you went to the mark scheme. You didn't practice the most important part of an exam - looking for and correcting your error.

Have you improved the speed of your algebra? $\mathbb{N O}$. You didn't try to complete each question in a fixed number of minutes so you still have no idea whether you were going at exam speed.

## This is what you should do:

1. Complete the exam paper in exam conditions. This means you continue working for two hours and make a real determined effort to find your errors before the time is up.
2. Don't use
a. The mark scheme
b. Your Survival Kit
c. Textbooks
d. Any other support
3. Mark the paper carefully using the mark scheme. Add up the marks and determine the grade.
4. Look at all the marks you lost - categorising them as being due to
a. $\mathrm{LU}=$ Lack of understanding (not knowing what to do)
b. $E E=A n$ expensive error (something that seems silly when you realise what you did)
5. Study your mistakes using
a. The mark scheme
b. Your Survival kit
c. Textbooks
d. Videos
e. etc.
6. Wait a day then repeat any question that you lost marks on using the strict timing (number of minutes = number of marks) and looking for your errors before you look at the mark scheme.
7. Repeat steps 3 and 4 over and over again until you are confident that if any of those questions are in your real exam, you will be able to do them quickly and accurately.

What has this process done to improve your chance of getting an improved grade in the real exam?

Do you have any more knowledge? YES. You kept going back to the harder questions until you could do them, so if these questions come up in your exam you, unlike some other students, can be confident you will know what to do.

Have you improved the accuracy of your algebra? YES. Not only have you practised finding errors during step one of the process, the fact that you have written them down and categorised them will help you to be more aware of the sorts of errors you make and this will help you, unlike other students, to avoid making them in the real exam.

Have you improved the speed of your algebra? YES. Every time you complete a paper (or question) in the correct time you are training yourself to be more comfortable working at the speed needed in the exam. This means that, unlike some other students, you won't have the problem of running out of time. The key to success is honest self-assessment followed by remedial action.

## Revision Tips

## Multiple attempts and crossing out

"Crossed-out work should be marked unless the candidate has replaced it with an alternative response." "Where a candidate has made multiple responses and indicates which response they wish to submit, examiners should mark this response. If there are several attempts at a question which have not been crossed out, examiners should mark the final answer which is the answer that is the most complete."

## Circle or highlight key phrases in questions.

Tick off question parts as you go so you don't leave any parts out Key phrases might include

| 3 d.p. | Hence | Exact Answer |
| :--- | :--- | :--- |
| Simplified Fraction | Nearest Integer | x is an integer, $\mathrm{x}>1$ | Write down

## Read the key phrases carefully

"Give an exact answer" means leave your answer with a fraction or $\pi$ or $\sqrt{ }$ or $\ln$ or $e$ in it. Don't give a rounded decimal.
"Hence" means use what you have just found out.
"Write down" means that there is no working - this shouldn't take you very long.
"Interpret" means that you need to write a sentence in the context of the question.

## Prove or Show

If you're asked to "Prove" or "Show" something, the last line in your working should state the answer. It's not just enough to write "As required" or "Q.E.D." - you must write out the statement.
E.g. $f(x)=2 x^{3}-7 x^{2}+4 x-4$. Use the factor theorem to show that $(x-2)$ is a factor of $f(x)$.
$\mathrm{f}(2)=2 \times 8-7 \times 4+4 \times 4-4=0$
$\therefore(x-2)$ is a factor of $\mathrm{f}(\mathrm{x})$
Therefore ( $x-2$ ) is a factor.

## Prove, Show, Verify

Prove means LHS $\equiv \cdots \equiv \cdots \equiv \cdots \equiv$ RHS
E.g. prove that $1+\tan ^{2} \theta \equiv \sec ^{2} \theta \ldots . . .$.
$\therefore$ Proof complete or QED
Don't take any shortcuts with proofs. Write out every step. You may know that $\frac{\tan \theta}{\sec \theta}=\sin \theta$ but if it's part of a proof, you must go through the intermediate step.

Show means use the information to get an answer
E.g. Show that $x=1.41$ is a solution to the equation $x^{2}=2$ correct to 3 s.f.
$\therefore x=1.41$ is a solution to the equation $x^{2}=2$
Verify means substitute a value
E.g. verify that $x=7$ is a solution to $x^{3}-2 x-329=0$

When $x=7, x^{3}-2 x-329=7^{3}-2 \mathrm{x} 7-329=343-14-329=0$
$\therefore x=7$ is a solution to $x^{3}-2 x-329=0$

## Scan the paper.

You can do the questions in any order. Start with all the familiar questions first. There may be questions that look unfamiliar. Do them last.

## Read the Question

Read the question after you've finished it, to check you've done what it asks you to.
(c) Substitute $x=\frac{1}{10}$ into your binomial expansion from part (a) and hence find an approximate value
for $\sqrt{ } 2$. Give your answer in the form $\frac{p}{q}$, where $p$ and $q$ are integers.

## Write on the exam paper

You can write on the exam paper. Draw diagrams to help you (e.g. area under a graph)
Do a sketch for those questions that involve tangents and normal. Don't try to hold the information in your head. If in doubt, sketch it out.
Write in black ink only. Don't use tippex or highlighters as your answer paper is scanned.

## Attempt every part of every question

If you can't do part (a) don't give up. Make up a value for your answer to part (a) and then use it in subsequent parts of the question to earn method marks.

## Improve Levels of Accuracy

Always write the full calculator display down first.
Then check the level of accuracy required in the question.
Assume 3 significant figures if no accuracy stated.
Always use unrounded answers in any subsequent calculations.
Remember $\mathrm{g}=9.8$

## Beware of taking shortcuts with your working.

$$
x^{2}+9 x+4=2(x-4)
$$

It doesn't take that long to write out an
intermediate step.

$$
x^{2}+7 x-4=0
$$

## Avoid basic arithmetic and algebraic errors.

$$
\begin{aligned}
& 5-(2-x)=3-x \\
& 3^{2}+5=11 \\
& 2+5(-1)^{3}=7
\end{aligned}
$$

## Check your work

In many questions, it's possible to take your answer and substitute values back in to the question. Use the differentiation and integration buttons.

## Know your Calculator!

## Angle units

Pure - radians unless you see the degrees sign ${ }^{\circ}$
Mechanics - normally degrees
Use brackets to tell the calculator the order of operations.
Use all the functions

- Statistics (mean, standard deviation)
- Distributions (Normal, Binomial)
- Solving quadratic equations
- Solving simultaneous equations
- Integration \& Differentiation


## Write in the correct space

Write within the space given for each question. Don't do question 5 in question 6's space as the papers are scanned in question by question. If you need additional paper ask for some. Label parts of questions clearly (a), (b), (c) etc.

## Timing

Don't spend too long on one question.
Keep a close eye on the time.
Put a watch on your desk rather than keep looking at the clock on the wall. (Buy a cheap watch if you don't have one.)
Make sure you know how many marks for each question and aim for a minute per mark.

## Use the correct notation

Integration

$$
\int \sin ^{2} x d x=\frac{1}{2} x-\frac{1}{4} \sin 2 x+c \quad \text { NOT } \quad \int \sin ^{2} x=\frac{1}{2} x-\frac{1}{4} \sin 2 x
$$

Differentiation

$$
y=3 x^{2} \quad \therefore \frac{d y}{d x}=6 x \quad \text { NOT } \quad \frac{d}{d x}=6 x
$$

## Formulae

Learn the formulae.
Quote the general form first then substitute in the correct values.
Make it clear what values you are substituting.

$$
\begin{gathered}
\text { e.g. } \quad \frac{d}{d x}\left(\frac{f(x)}{g(x)}\right)=\frac{f^{\prime}(x) g(x)-f(x) g^{\prime}(x)}{(g(x))^{2}} \\
\frac{d}{d x}\left(\frac{e^{2 x}}{\cos x}\right)=\frac{2 e^{2 x} \cos x-e^{2 x}(-\sin x)}{\cos ^{2} x} \\
\text { When } \mathrm{x}=0, \quad \frac{\mathrm{dy}}{\mathrm{dx}}=\frac{2+0}{1}=2
\end{gathered}
$$

## Learn The Formulae (these are in the specification)

## Appendix 1: Formulae

Formulae that students are expected to know for $A$ Level Mathematics are given below and will not appear in the booklet Mathematical Formulae and Statistical Tables, which will be provided for use with the paper.

Pure Mathematics
Quadratic Equation
$a x^{2}+b x+c=0$ has roots $\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}$
Laws of Indices
$a^{x} a^{x} \equiv a^{x+y}$
$a^{x} \div a^{y} \equiv a^{x-3}$
( $\left.a^{a}\right)^{y} \equiv a^{n}$
Laws of Logarithms
$x=a^{n} \ominus n=\log _{a} x$ for $a>0$ and $x>0$
$\log _{a} x+\log _{a} y \equiv \log _{a}(x y)$
$\log _{a} x-\log _{a} y \equiv \log _{a}\left(\frac{x}{y}\right)$
$k \log _{a} x \equiv \log _{a}\left(x^{k}\right)$
Coordinate Geometry
A straight line graph, gradient $m$ passing through $\left(x_{1}, y_{1}\right)$ has equation $y-y_{1}=m\left(x-x_{1}\right)$
Straight lines with gradients $m_{1}$ and $m_{2}$ are perpendicular when $m_{1} m_{2}=-1$

Sequences
Seneral term of an arithmetic progression:
$u_{n}=a+(n-1) d$
General term of a geometric progression:
$u_{n}=a r^{n-1}$

Vectors
$|x i+y j+z k|=\sqrt{\left(x^{2}+y^{2}+z^{2}\right)}$

Statistics
The mean of a set of data: $x=\frac{\sum x}{n}=\frac{\sum \mathrm{fx}}{\sum \mathrm{f}}$

The standard Normal variable: $Z=\frac{X-\mu}{\sigma}$ where $X \sim \mathrm{~N}\left(\mu, \sigma^{2}\right)$

## Mechanics

Forces and Equilibrium
Weight $=$ mass $\times g$
Friction: $F \leqslant \mu R$
Newton's second law in the form: $F=m a$

Kinematics
For motion in a straight line with variable acceleration:
$v=\frac{\mathrm{d} r}{\mathrm{~d} t} \quad a=\frac{\mathrm{d} v}{\mathrm{~d} t}=\frac{\mathrm{d}^{2} r}{\mathrm{~d} t^{2}}$
$r=\int v \mathrm{~d} t \quad v=\int a \mathrm{~d} t$
$f(g(x)) g^{\prime}(x) \quad f(g(x))+c$
Area under a curve $=\int y \mathrm{~d} x(y \geqslant 0)$

Trigonometry
In the triangle $A B C$
Sine rule: $\quad \frac{a}{\sin A}=\frac{b}{\sin B}=\frac{c}{\sin C}$
Cosine rule: $\quad a^{2}=b^{2}+c^{2}-2 b c \cos A$
Area $=\frac{1}{2} a b \sin C$
$\cos ^{2} A+\sin ^{2} A \equiv 1$
$\sec ^{2} A \equiv 1+\tan ^{2} A$
$\operatorname{cosec}^{2} A \equiv 1+\cot ^{2} A$
$\sin 2 A \equiv 2 \sin A \cos A$
$\cos 2 A \equiv \cos ^{2} A-\sin ^{2} A$
$\tan 2 A \equiv \frac{2 \tan A}{1-\tan ^{2} A}$
Mensuration
Circumference and area of circle, radius $r$ and diameter $d$
$C=2 \pi r=\pi d \quad A=\pi r^{2}$
Pythagoras' theorem:
In any right-angled triangle where $a, b$ and $c$ are the lengths of the sides and $c$ is the
hypotenuse, $c^{2}=a^{2}+b^{2}$
Area of a trapezium $=\frac{1}{2}(a+b) h$, where $a$ and $b$ are the lengths of the parallel sides and $h$
is their perpendicular separation.
Volume of a prism $=$ area of cross section $\times$ length
For a circle of radius $r$, where an angle at the centre of $\theta$ radians subtends an arc of length $s$
and encloses an associated sector of area $A$ :
$s=r \theta \quad A=\frac{1}{2} r^{2} \theta$

## Make sure you know your way around the formula book

## Pure Mathematics

Mensuration
Surface area of sphere $=4 \pi r^{2}$
Area of curved surface of cone $=\pi r \times$ slant height
Arithmetic series
$S_{n}=\frac{1}{2} n(a+l)=\frac{1}{2} n[2 a+(n-1) d]$

Binomial series
$(a+b)^{n}=a^{n}+\binom{n}{1} a^{n-1} b+\binom{n}{2} a^{n-2} b^{2}+\ldots+\binom{n}{r} a^{n-1} b^{r}+\ldots+b^{n} \quad(n \in \mathbb{N})$
where $\binom{n}{r}={ }^{n} \mathrm{C}_{r}=\frac{n!}{r!(n-r)!}$
$(1+x)^{n}=1+n x+\frac{n(n-1)}{1 \times 2} x^{2}+\ldots+\frac{n(n-1) \ldots(n-r+1)}{1 \times 2 \times \ldots \times r} x^{r}+\ldots \quad(|x|<1, n \in \mathbb{R})$

Logarithms and exponentials
$\log _{a} x=\frac{\log _{b} x}{\log _{b} a}$
$\mathrm{e}^{x \mathfrak{m} a}=a^{x}$
Geometric series
$S_{n}=\frac{a\left(1-r^{n}\right)}{1-r}$
$S_{\infty}=\frac{a}{1-r}$ for $|r|<1$

Trigonometric identities
$\sin (A=B)-\sin A \cos B=\cos A \sin B$
$\cos (A \pm B)-\cos A \cos B \mp \sin A \sin B$
$\tan (A \neq B)-\frac{\tan A \pm \tan B}{1 \mp \tan A \tan B} \quad\left(A \pm B=\left(k+\frac{2}{3}\right) \pi\right)$
$\sin A+\sin B-2 \sin \frac{A+B}{2} \cos \frac{A-B}{2}$
$\sin A-\sin B-2 \cos \frac{A+B}{2} \sin \frac{A-B}{2}$
$\cos A+\cos B-2 \cos \frac{A+B}{2} \cos \frac{A-B}{2}$
$\cos A-\cos B=-2 \sin \frac{A+B}{2} \sin \frac{A-B}{2}$
Semall angle approximations
$\sin \theta=\theta$
$\cos \theta=1-\frac{\theta^{2}}{2}$
$\tan \theta \approx \theta$
where $\theta$ is measured in radians
Differentiation
Fiost Principles
$f^{\prime}(x)=\lim _{b \rightarrow 0} \frac{f(x+h)-f(x)}{h}$

| $f(x)$ | $f^{\prime}(x)$ |
| :--- | :--- |
| $\tan k x$ | $k \sec ^{2} k x$ |
| $\sec k x$ | $k \sec ^{k x} \tan k x$ |
| $\cot k x$ | $-k \operatorname{cosec}^{2} k x$ |
| $\operatorname{cosec} k x$ | $-k \operatorname{cosec} k x \cot k x$ |
| $\frac{f(x)}{g(x)}$ | $\frac{f^{\prime}(x) g(x)-f(x) g^{\prime}(x)}{(g(x))^{2}}$ |

```
Standard deviation
Standard deviation = v(Variance)
Interquartile range = IQR = Q - - Q 
for a set of }n\mathrm{ values }\mp@subsup{x}{1}{},\mp@subsup{x}{2}{},\ldots\mp@subsup{x}{p}{},\ldots\mp@subsup{x}{n}{
S Sn=\Sigma(x,-x\mp@subsup{)}{}{2}=\Sigma\mp@subsup{x}{i}{2}-\frac{(\Sigma\mp@subsup{x}{i}{\prime}\mp@subsup{)}{}{2}}{n}
Standard deviation =\sqrt{}{\frac{\mp@subsup{S}{x}{\prime}}{n}}\mathrm{ or }\sqrt{}{\frac{\sum\mp@subsup{x}{}{2}}{n}-\mp@subsup{\overline{x}}{}{2}}\mathrm{ ,}
```

| Distribution of $X$ | $\mathrm{P}(X=x)$ | Mean | Variance |
| :--- | :---: | :---: | :---: |
| Binomial $\mathrm{B}(n, p)$ | $\binom{n}{x} p^{x}(1-p)^{-x}$ | $n p$ | $n p(1-p)$ |

Sampling distributions
For a random sample of $n$ observations from $\mathrm{N}\left(\mu, \sigma^{2}\right)$
$\frac{\bar{X}-\mu}{\sigma / \sqrt{n}} \sim \mathrm{~N}(0,1)$
statistical tables
The following statistical tables are required for $A$ Level Mathematics:
Binomial Cumulative Distribution Function (see page 29)
(see page 34)
Values for Correlationefficients: Product Moment Coefficient (see page 37)
Random Numbers (see page 38)
Mechanics
Kinematics
$v=u+a t$
$s=u t+\frac{1}{2} a t^{2}$
$s=v t-\frac{1}{2} a t^{2}$
$v^{2}=u^{2}+2 a s$
$s=\frac{1}{2}(u+v) t$

A Level Maths Exam Practice Chart


Page | 11

