| Question |  | Oٍ | 苼 |  | Topic | Comment |
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| 部 | Aa |  |  |  | C4 Integration | $\frac{2}{3} \sin \frac{3}{2} x+c$ |
|  | Ab |  |  |  | C4 Integration | $\tan x+c$ |
|  | Ac |  |  |  | C4 Integration | $-\frac{1}{3} \cot 3 x+c$ |
|  | Ba |  |  |  | C3 Modulus solves | $\frac{1}{6} \text { and } \frac{7}{4}$ |
|  | Bb |  |  |  | C3 Modulus solves | -3, 2 |
|  | Bc |  |  |  | C3 Modulus solves | $-\frac{5}{8}, \frac{5}{2}$ |
|  | Bd |  |  |  | C3 Modulus solves | $\frac{1}{4}, 3$ |
|  | Be |  |  |  | C3 Modulus solves | $\pm 1, \pm 4$ |
|  | Ca |  |  |  | C4 Binomial Expansion (simple) | $\frac{1}{2}-\frac{1}{4} x+\frac{1}{8} x^{2}-\frac{1}{16} x^{3}+\cdots,\|x\|<2$ |
|  | Cb |  |  |  | C4 Binomial Expansion (simple) | $\frac{1}{27}+\frac{1}{27} x+\frac{2}{81} x^{2}+\frac{10}{729} x^{3}+\cdots\|x\|$ <br> $<3$ |
|  | Cc |  |  |  | C4 Binomial Expansion (simple) | $2-2 x-2 x^{2}-\frac{10}{3} x^{3}+\cdots,\|x\|<\frac{1}{3}$ |
|  | Cd |  |  |  | C4 Binomial Expansion (simple) | $\frac{1}{2}-\frac{3}{8} x+\frac{27}{64} x^{2}-\frac{135}{256} x^{3}+\cdots,\|x\|<\frac{2}{3}$ |
|  | Da |  |  |  | C4 Partial Fractions | $\frac{1}{x+2}+\frac{1}{x+3}$ |
|  | Db |  |  |  | C4 Partial Fractions | $\frac{4}{x}-\frac{2}{x^{2}}+\frac{3}{x+1}$ |
|  | Dc |  |  |  | C4 Partial Fractions | $\frac{5}{x+2}-\frac{4}{x+3}$ |
|  | MEAi |  |  |  | Trig | $\frac{2 p}{1+p^{2}}$ |
|  | MEAii |  |  |  | Trig | $\frac{1-p^{2}}{1+p^{2}}$ |
|  | MEAiii |  |  |  | Trig | $\frac{2 p}{1-p^{2}}$ |
|  | MEB |  |  |  | Trig | R.H.S. $\begin{aligned} & =\frac{1-\tan ^{2}\left(\frac{\theta}{2}\right)}{1+\tan ^{2}\left(\frac{\theta}{2}\right)}=\frac{1-\tan ^{2}\left(\frac{\theta}{2}\right)}{\sec ^{2}\left(\frac{\theta}{2}\right)} \\ & =\cos ^{2}\left(\frac{\theta}{2}\right)\left\{1-\tan ^{2}\left(\frac{\theta}{2}\right)\right\} \\ & =\cos ^{2}\left(\frac{\theta}{2}\right)-\sin ^{2}\left(\frac{\theta}{2}\right)=\cos \theta=\text { L.H.S } \end{aligned}$ |



| $\alpha$ | $\beta$ | $\gamma$ | $\delta$ | $\varepsilon$ | $\zeta$ | $\eta$ | $\theta$ | $\imath$ | $\kappa$ | $\lambda$ | $\mu$ | $v$ | $\xi$ | $o$ | $\pi$ | $\rho$ | $\sigma$ | $\tau$ | $v$ | $\varphi$ | $\chi$ | $\psi$ | $\omega$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

"The mathematician has reached the highest rung on the ladder of human thought" H Ellis

## A2 Maths with Mechanics Assignment $\kappa$ (kappa) Due in w/b 28/11

## Drill

Part A Integrate with respect to $x$ : use the correct notation
(a) $\cos \frac{3 x}{2}$
(b) $\sec ^{2} x$
(c) $\operatorname{cosec}^{2} 3 x$

Part B Solve the following equations: graphically or otherwise
(a) $|5 x-4|=|x+3|$
(b) $\left|x^{2}+x\right|=6$
(c) $|3 x+5|=|5 x|$
(d) $\quad|6 x-7|=|2 x+5|$
(e) $\quad\left|x^{2}-4\right|=3|x|$

Part C Expand each of the following in ascending powers of $x$ up to and including the term in $x^{3}$ and state the set of values of $x$ for which each expression is valid.
(a) $(2+x)^{-1}$
(b) $(3-x)^{-3}$
(c) $(8-24 x)^{\frac{1}{2}}$
(d) $(4+6 x)^{-\frac{1}{2}}$

Part D Express as partial fractions:
(a) $\frac{2 x+5}{(x+2)(x+3)}$
(b) $\frac{7 x^{2}+2 x-2}{x^{2}(x+1)}$
(c) $\frac{x+7}{x^{2}+5 x+6}$

## Focus from C3 Mock Exam

MEA) Given $\tan x=p$, find in terms of $p$ :
i) $\sin 2 x$
ii) $\cos 2 x$
iii) $\tan 2 x$

MEB) Show that: $\cos \theta \equiv \frac{1-\tan ^{2} \frac{\theta}{2}}{1+\tan ^{2} \frac{\theta}{2}}$
MEC) Show that $\sin \theta \equiv \frac{2 \tan \frac{\theta}{2}}{1+\tan ^{2} \frac{\theta}{2}}$

## Current work M2

1. A particle P is projected from a point O on level ground with speed $50 \mathrm{~ms}^{-1}$ at an angle $\Theta$ where
$\sin \theta=\left(\frac{7}{25}\right)$ above the horizontal. Find
a) the height of $P$ at the point where its horizontal displacement from 0 is 120 m ,
b) the speed of $P$ two seconds after projection,
c) the times after projection at which $P$ is moving at an angle of $\tan ^{-1}\left(\frac{1}{4}\right)$ to the ground
2. David kicks a ball on a level field with a speed of $20 \mathrm{~ms}^{-1}$ at an angle of $30^{\circ}$ to the horizontal.
(a) How far away from him does the ball land?
(b) How high does the ball reach?
3. A cricket ball, which may be modelled as a particle moving freely under gravity, is struck from a height of 0.5 m above a horizontal field with a velocity of $26 \mathrm{~ms}^{-1}$ at an angle $\alpha$ above the horizontal, where $\tan \alpha=5 / 12$.
(a) The fielders can reach up to a height of 2.5 m . Between what times is the ball out of reach of the fielders?
(b) The captain wishes his fielders to catch the ball as soon as it is within reach. How far from the bat should the fielders be placed in order to do this?
4. 



A golf ball is struck from the point $T$, at the top of a cliff 49 m above sea level, with a speed of $14 \mathrm{~m} \mathrm{~s}^{-1}$ at an angle of $45^{\circ}$ to the horizontal, as shown in the diagram. The point $O$ is at sea level and vertically below $T$. The point $A$ is the highest point reached by the ball in its motion. The ball strikes the sea at the point $B$.
(a) Find the height $A$ above sea level.
(b) Find the distance $O B$.
5. A stone thrown from a height of 2 m just clears a 6 m high wall that is 10 m away. Show that the relationship between the speed of projection V and the angle of projection to the horizontal $\theta$ can be given by

$$
V^{2}=\frac{490}{(10 \tan \theta-4) \cos ^{2} \theta}
$$

## Consolidation

6. Integrate the following w.r.t. $x$ :
(a) $\int 3 e^{4 x+2} d x$
(b) $\int\left(4 e^{4-x}+2\right) d x$
(c) $\int \frac{e^{2 x}+1}{4 e^{-x}} d x$ hint: split into $\frac{e^{2 x}}{4 e^{-x}}+\frac{1}{4 e^{-x}}$
7. Given that $\sin A=\frac{4}{5}, 0<A<90^{\circ}$ and that $\cos B=\frac{2}{3}, 0<B<90^{\circ}$, find without using a calculator the value of
(a) $\quad \tan \mathrm{A}$
(b) $\quad \sin B$
(c) $\quad \cos (\mathrm{A}+\mathrm{B})$
(d) $\quad \sin (A+B)$
8. Prove the following identities:
(a) $\frac{1}{\cos A+\sin A}+\frac{1}{\cos A-\sin A} \equiv \tan 2 A \operatorname{cosec} A$
(b) $\cos (A+B)-\cos (A-B) \equiv-2 \sin A \sin B$
9. A curve has the equation $\mathrm{y}=3^{x}$.

Find an equation for the tangent to the curve at the point $(2,9)$
10. Show that the curve with equation $y=\frac{\ln x}{x}$ has a maximum value of $\frac{1}{e}$ at $x=e$.
11. $\mathrm{f}(x)=x^{3}+x^{2}-4 x-1$. The equation $\mathrm{f}(x)=0$ has only one positive root, $\alpha$.
(a) Show that $\mathrm{f}(x)=0$ can be rearranged as $x=\sqrt{\left(\frac{4 x+1}{x+1}\right)}, x \neq-1$.

The iterative formula $x_{n+1}=\sqrt{\left(\frac{4 x_{n}+1}{x_{n}+1}\right)}$ is used to find an approximation to $\alpha$.
(b) Taking $x_{1}=1$, find, to 2 decimal places, the values of $x_{2}, x_{3}$ and $x_{4}$.
(c) Prove that $\alpha=1.70$, is correct to 2 dp .
12. (a) Express $3 \cos \theta+4 \sin \theta$ in the form $R \cos (\theta-\alpha)$, where $R>0$ and $0<\alpha<\frac{\pi}{2}$
(b) Given that the function f is defined by $f(\theta) \equiv 1-3 \cos 2 \theta-4 \sin 2 \theta, \theta \in \mathbb{R}, 0 \leq \theta \leq \pi$
i) state the range of $f$,
ii) solve the equation $f(\theta)=0$
(c) Find the coordinates of the turning points of the curve with equation $y=\frac{2}{3 \cos x+4 \sin x}$ in the interval $[0,2 \pi]$.
13. (a) Express $\frac{x-2}{(1-x)(1-2 x)}$ in partial fractions.
(b) Hence find the series expansion of $\frac{x-2}{(1-x)(1-2 x)}$ in ascending powers of x up to and including the term in $x^{3}$ and state the set of values of x for which the expression is valid.

