

# BHASVIC MαTHS

## A1 DOUBLES ASSIGNMENT 17B

### Skills 1

Find any point(s) of inflection of the following functions.

(a)  $f(x) = \cos^2 x - 2 \sin x, 0 < x < 2\pi$

(b)  $f(x) = -\frac{x^3 - 2x^2 + x - 1}{x - 2}, x \neq 2$

(c)  $f(x) = -\frac{x^3}{x^2 - 4}, x \neq \pm 2$

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### Skills 2

Now, Integrate the following functions using an appropriate method when required:

(a)  $\int -\sin(3x + 1) dx$

(b)  $\int 4 \cos\left(\frac{x}{2}\right) dx$

(c)  $\int \tan x dx$

(d)  $\int \cot 4x dx$

(e)  $\int \sec^5 2x \tan 2x dx$

(f)  $\int \tan 5x dx$

(g)  $\int \sin^2 6x dx$

(h)  $\int 3\cos^2 2x dx$

(i)  $\int 3\tan^2 4x dx$

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### Skills 1 - Answers

(a)  $\left(\frac{\pi}{6}, -\frac{1}{4}\right), \left(\frac{5\pi}{6}, -\frac{1}{4}\right)$

(b) (1, -1)

(c) (0, 0)

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### Skills 2 – Answers

(a)  $\frac{1}{3}\cos(3x + 1) + c$

(b)  $8\sin\left(\frac{x}{2}\right) + c$

(c)  $-\ln(\cos x) + c$

(d)  $\frac{1}{4}\ln(\sin 4x) + c$

(e)  $\frac{1}{10}\sec^5 2x + c$

(f)  $-\frac{1}{5}\ln(\cos 5x) + c$

(g)  $\frac{1}{2}x - \frac{1}{24}\sin 12x + c$

(h)  $\frac{3}{2}x + \frac{3}{8}\sin 4x + c$

(i)  $\frac{3}{4}\tan 4x - 3x + c$

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1

The curve  $C$  has equation  $y = xe^x$ .

- (a) Find the exact coordinates of the stationary point on  $C$  and determine its nature.
- (b) Find the coordinates of any non-stationary points of inflection on  $C$ .
- (c) Hence sketch the graph of  $y = xe^x$

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## A1 DOUBLES ASSIGNMENT 17B

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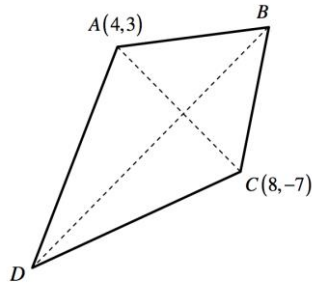
- (a) Sketch the two inequalities  $y < 9 - x^2$  and  $y \geq x^2 - 3x + 4$
- (b) Shade the region that satisfies both inequalities

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The figure shows a kite ABCD where the vertices A and C have coordinates (4,3) and (8,-7) respectively.

The diagonal BD is a line of symmetry of the kite.

Find an equation for the diagonal BD

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- (a) A particle is projected upwards with a speed of  $14 \text{ m s}^{-1}$ . Find for how long it is above 2 m.
- (b) A ball is thrown vertically upwards from a height 1.6m above the ground, with a speed of  $7 \text{ m s}^{-1}$ . Find the speed when it hits the ground.

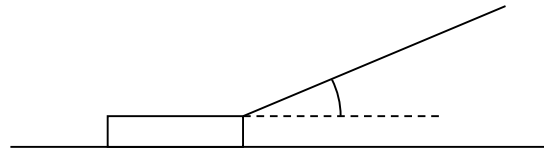
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A sledge has mass 30 kg. The sledge is pulled in a straight line along horizontal ground by means of a rope. The rope makes an angle  $20^\circ$  with the horizontal, as shown in Figure 3. The coefficient of friction between the sledge and the ground is 0.2. The sledge is modelled as a particle and the rope as a light inextensible string. The tension in the rope is 150 N. Find, to 3 significant figures,

- (a) the normal reaction of the ground on the sledge,
- (b) the acceleration of the sledge

When the sledge is moving at  $12 \text{ m s}^{-1}$ , the rope is released from the sledge.

- (c) Find, to 3 significant figures, the distance travelled by the sledge from the moment when the rope is released to the moment when the sledge comes to rest.

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### NEW TECHNIQUES!

Given that the displacement  $s$  for a particle at time  $t$  seconds moving in a straight line is given by

$$s = t^3 + 4t + 6$$

Where  $v$  is the velocity in  $\text{ms}^{-1}$  and  $a$  is the acceleration in  $\text{ms}^{-2}$  and given that

$$v = \frac{ds}{dt} \text{ and } a = \frac{d^2s}{dt^2}. \text{ Find:}$$

expressions for  $v$  and  $a$  terms of  $t$ ,  
the displacement, velocity and acceleration when  $t=2$ .

*Only zero and positive values of  $t$  should be considered.*

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## A1 DOUBLES ASSIGNMENT 17B

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Two helicopters  $P$  and  $Q$  are moving in the same horizontal plane. They are modelled as particles moving in straight lines with constant speeds. At noon  $P$  is at the point with position vector  $(20\mathbf{i} + 35\mathbf{j})$  km with respect to a fixed origin  $O$ . At time  $t$  hours after noon the position vector of  $P$  is  $\mathbf{p}$  km. When  $t = \frac{1}{2}$  the position vector of  $P$  is  $(50\mathbf{i} - 25\mathbf{j})$  km. Find

- (a) the velocity of  $P$  in the form  $(a\mathbf{i} + b\mathbf{j})$  km h<sup>-1</sup>,
- (b) an expression for  $\mathbf{p}$  in terms of  $t$ .

At noon  $Q$  is at  $O$  and at time  $t$  hours after noon the position vector of  $Q$  is  $\mathbf{q}$  km. The velocity of  $Q$  has magnitude 120 km h<sup>-1</sup> in the direction of  $4\mathbf{i} - 3\mathbf{j}$ . Find

- (c) an expression for  $\mathbf{q}$  in terms of  $t$ ,
- (d) the distance, to the nearest km, between  $P$  and  $Q$  when  $t = 2$ .

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A curve C has equation  $y = \frac{1}{2}e^{2x} - 4x + 1, \quad x \in \mathbb{R}$

The point P lies on C where  $x = \ln 4$ .

(a) Show that the equation of the tangent to the curve is  $y = 12x + 9 - 32 \ln 2$

The point Q lies on C where  $x = \ln 2$ .

The normal to the curve at the point Q meets the tangent to the curve at the point P, at the point R.

(b) Show that the co-ordinates of R are  $(\ln 2, 9 - 20 \ln 2)$

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The radius,  $r$  cm, of a circle is increasing at the constant rate of  $3 \text{ cm s}^{-1}$   
Find the rate at which the area of the circle is increasing when its radius is  
13.5 cm.

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## A1 DOUBLES ASSIGNMENT 17B

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A circle has parametric equations  $x = 4 \sin t - 3$ ,  $y = 4 \cos t + 5$ .

- (a) Find the Cartesian equation of the circle
- (b) Draw a sketch of the circle
- (c) Find the exact coordinates of the points of intersection of the circle with the y axis

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## A1 DOUBLES ASSIGNMENT 17B

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(a) Show that  $\cos^4 x \equiv \frac{1}{8} \cos 4x + \frac{1}{2} \cos 2x + \frac{3}{8}$

(b) Hence find  $\int \cos^4 x \, dx$

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## A1 DOUBLES ASSIGNMENT 17B

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(a) Given  $f(x) = \frac{x}{x+3} - \frac{x+24}{2x^2+5x-3}$ , show that  $f(x) = \frac{2(x-4)}{2x-1}$

(b) Find  $f^{-1}(x)$

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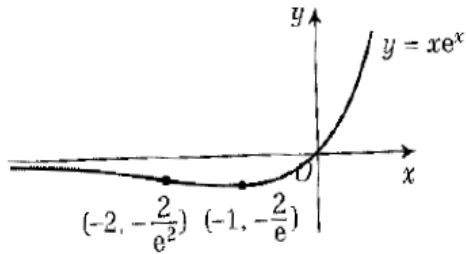
## A1 DOUBLES ASSIGNMENT 17B

### 1 - Answers

(a)  $\left(-1, -\frac{1}{e}\right)$ , minimum

(b)  $\left(-2, -\frac{2}{e^2}\right)$

(c)



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**BHASVIC MαTHS**  
**A1 DOUBLES ASSIGNMENT 17B**

2 - Answers

Sketch

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## A1 DOUBLES ASSIGNMENT 17B

### 3 - Answers

$$5y = 2x - 22$$

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## A1 DOUBLES ASSIGNMENT 17B

### 4 - Answers

(a) 2.56 seconds

(b)  $9.0\text{ms}^{-1}$

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### 5 - Answers

(a) 243N

(b)  $3.08\text{ms}^{-2}$

(c) 36.7m

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### 6 - Answers

(a)  $v=3t^2+4$ ,  $a=6t$

(b)  $22\text{m}$ ,  $16\text{m}^{-1}$ ,  $12\text{ms}^{-2}$

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# BHASVIC MαTHS

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### 7 - Answers

(a)  $60\mathbf{i} - 120\mathbf{j}$

(b)  $\mathbf{p} = 20\mathbf{i} + 35\mathbf{j} + (60\mathbf{i} - 120\mathbf{j})t$

(c)  $\mathbf{q} = 96t\mathbf{i} - 72t\mathbf{j}$

(d) 80 km

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**BHASVIC MαTHS**  
**A1 DOUBLES ASSIGNMENT 17B**

8 - Answers

Proof

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**BHAVIC MATHS**  
**A1 DOUBLES ASSIGNMENT 17B**

9 - Answers

$$81\pi \text{ cm}^2\text{s}^{-1}$$

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# BHASVIC MαTHS

## A1 DOUBLES ASSIGNMENT 17B

### 10 - Answers

(a)  $(x + 3)^2 + (y - 5)^2 = 16$

(b) check desmos

(c)  $(0, 5 + \sqrt{7}), (0, 5 - \sqrt{7})$

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# BHASVIC MATHS

## A1 DOUBLES ASSIGNMENT 17B

### 11 - Answers

$$\begin{aligned} \text{(a) } \cos^4 x &= (\cos^2 x)^2 = \left(\frac{1+\cos 2x}{2}\right)^2 = \frac{1}{4} + \frac{1}{2}\cos 2x \\ &+ \frac{1}{4}\cos^2 2x = \frac{1}{4} + \frac{1}{2}\cos 2x + \frac{1}{4}\left(\frac{1+\cos 4x}{2}\right) \\ &= \frac{3}{8} + \frac{1}{2}\cos 2x + \frac{1}{8}\cos 4x \end{aligned}$$

$$\text{(b) } \frac{1}{32}\sin 4x + \frac{1}{4}\sin 2x + \frac{3}{8}x + c$$

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**BHASVIC MαTHS**  
**A1 DOUBLES ASSIGNMENT 17B**

12 - Answers

(a) Proof

(b)  $\frac{(x-8)}{2x-2}$

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