

BHASVIC MATHS

A1 DOUBLES ASSIGNMENT 20B

1

Use the substitutions given to find:

(a) $\int x\sqrt{1+x} \, dx; u = 1+x$

(b) $\int \frac{1+\sin x}{\cos x} \, dx; u = \sin x$

(c) $\int \sin^3 x \, dx; u = \cos x$

(d) $\int \frac{2}{\sqrt{x}(x-4)} \, dx; u = \sqrt{x}$

(e) $\int \sec^2 x \tan x \sqrt{1+\tan x} \, dx; u^2 = 1+\tan x$

(f) $\int \sec^4 x \, dx; u = \tan x$

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2

Find the following integrals

(a) $\int 3 \ln x \, dx$

(b) $\int x \ln x \, dx$

(c) $\int \frac{\ln x}{x^3} \, dx$

(d) $\int (\ln x)^2 \, dx$

(e) $\int (x^2 + 1) \ln x \, dx$

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1

(a) Find the set of values of u that satisfy $\frac{3}{u^2} + 2 \leq \frac{-7}{u}, u \neq 0$

(b) Hence find the set of values of u that satisfy $\frac{3}{(u-1)^2} + 2 \leq \frac{-7}{(u-1)}, u \neq 0$

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2

A ball is thrown in the air. After t seconds, its height, s , in metres above the ground is given by the equation $2s = -10t^2 + 16t + 3$.

- (a) Find t when the ball is 4.5 metres above the ground.
- (b) Show that $s = a(t + b)^2 + c$ where a , b and c are constants to be found.
- (c) Hence find the maximum height of the ball and the value of t for which this occurs.

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3

Solve the following inequalities

(a) $\left| \frac{x-1}{x-2} \right| \geq 4$

(b) $\left| \frac{2p^2}{3p+2} \right| < 1$

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4

The points A, B, C and D have co-ordinates $(-5,6)$ and $(5,1)$ and $(8,3)$ and $(k,-13)$, respectively, where k is a constant.

- (a) Find an equation of the straight line through A and B.
- (b) Given that CD is perpendicular to AB, find the value of k

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5

A smooth bead Y is threaded on a light inextensible string. The ends of the string are attached to two fixed points X and Z on the same horizontal level. The bead is held in equilibrium by a horizontal force of magnitude 8N acting parallel to ZX. The bead Y is vertically below X and angle $XZY = 30^\circ$. Find (a) the tension in the string, (b) the weight of the bead.

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6

A particle P is projected with velocity $(3u\mathbf{i} + 4u\mathbf{j}) \text{ m s}^{-1}$ from a fixed point O on a horizontal plane. Given that P strikes the plane at a point 750 m from O ,

- (a) show that $u = 17.5$,
- (b) calculate the greatest height above the plane reached by P ,
- (c) find the angle the direction of motion of P makes with \mathbf{i} when $t = 5$.

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7

The curve C has equation $y = \frac{x}{x^2+1}$

- (a) Show that there is no point on C where the gradient is -1
- (b) Find the co-ordinates of the points on C where the gradient is $\frac{12}{25}$

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8

(a) A curve has parametric equations $x = t^2 - 1$, $y = t - t^3$. Draw this curve for when $-2 \leq t \leq 2$.

(b) Find the Cartesian equation of the curve when $t > 0$

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8b

The curve C shown in Figure 4 has parametric equations

#

$$x = 1 + \sqrt{3} \tan \theta, \quad y = 5 \sec \theta, \quad -\frac{\pi}{2} < \theta < \frac{\pi}{2}$$

The curve C crosses the y -axis at A and has a minimum turning point at B , as shown in Figure 4.

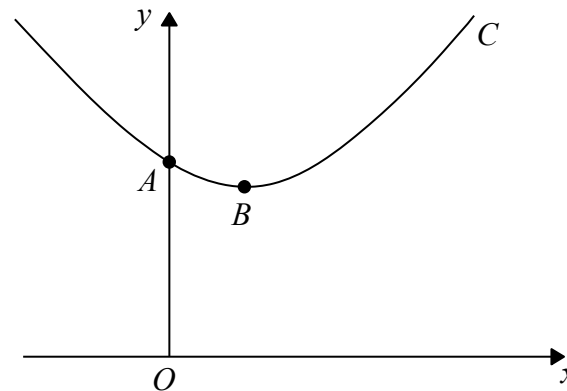


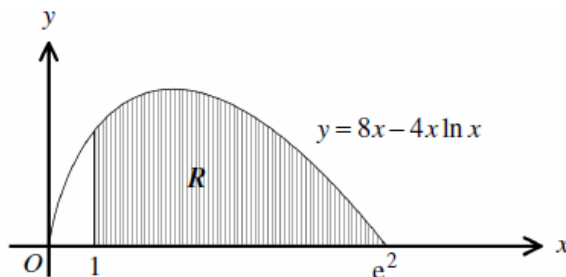
Figure 4

- Find the exact coordinates of A .
- Show that $\frac{dy}{dx} = \lambda \sin \theta$, giving the exact value of the constant λ
- Find the coordinates of B .
- Show that the Cartesian equation for the curve C can be written in the form $y = k\sqrt{(x^2 - 2x + 4)}$ where k is a simplified surd to be found.

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The figure above shows the graph of the curve with equation

$$y = 8x - 4x \ln x, 0 < x \leq e^2$$

The region R is bounded by the curve, the x axis and the line with equation $x = 1$

Determine the exact area of R

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11

Using a suitable trigonometric substitution for x , find $\int_{\frac{1}{2}}^{\frac{\sqrt{3}}{2}} x^2 \sqrt{1-x^2} dx$

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11b

Find:

$$\int \frac{3-x}{2x^3-x^2} dx$$

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12

Complete this old spec paper

https://www.madasmaths.com/archive/iygb_practice_papers/c4_practice_papers/c4_m.pdf

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Skills 1 - Answers

(a) $\frac{2}{5}(1+x)^{\frac{5}{2}} - \frac{2}{3}(1+x)^{\frac{3}{2}} + c$

(b) $-\ln|1 - \sin x| + c$

(c) $\frac{\cos^3 x}{3} - \cos x + c$

(d) $\ln \left| \frac{\sqrt{x}-2}{\sqrt{x}+2} + c \right|$

(e) $\frac{2}{5}(1 + \tan x)^{\frac{5}{2}} - \frac{2}{3}(1 + \tan x)^{\frac{3}{2}} + c$

(f) $\tan x + \frac{1}{3}\tan^3 x + c$

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Skills 2 – Answers

(a) $3x \ln x - 3x + c$

(b) $\frac{x^2}{2} \ln x - \frac{x^2}{4} + c$

(c) $-\frac{\ln x}{2x^2} - \frac{1}{4x^2} + c$

(d) $x(\ln x)^2 - 2x \ln x + 2x + c$

(e) $\frac{x^3}{3} \ln x - \frac{x^3}{9} + x \ln x - x + 3$

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1 - Answers

(a) $-3 \leq u \leq \frac{-1}{2}$ (you must include a sketch)

(b) $-2 \leq u \leq \frac{1}{2}$

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2 - Answers

(a) $t = \frac{3}{5}$ or $t = 1$

(b) $a = -5, b = \frac{4}{5}, c = 4.7$

(c) Max is 4.7 metres when $t = 0.8$ seconds.

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3 - Answers

(a) $\frac{9}{5} \leq x \leq \frac{7}{3}$

(b) $-\frac{1}{2} < p < 2$

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4 - Answers

(a) $x + 2y = 7$

(b) $k = 0$

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5 - Answers

(a) $T=9.24\text{N}$ (3sf)

(b) 13.9N (3sf)

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6 - Answers

(b) 250 m

(c) 21.8°

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7 - Answers

(b) $\left(\frac{1}{2}, \frac{2}{5}\right)$ and $\left(-\frac{1}{2}, -\frac{2}{5}\right)$

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8 - Answers

(a) Check desmos

(b) $y = \sqrt{x + 1} - (\sqrt{x + 1})^3$

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9 - Answers

(a) $A\left(0, \frac{10\sqrt{3}}{3}\right)$

(b) $\lambda = \frac{5}{\sqrt{3}}$

(c) $B(1, 5)$

(d) $k = \frac{5\sqrt{3}}{3}$

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10 - Answers

$$e^4 - 5$$

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11 - Answers

$$\frac{2\pi+3\sqrt{3}}{96}$$

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BHAVIC MATHS
A1 DOUBLES ASSIGNMENT 20B

12 - Answers

$$-5 \ln|x| + 3x^{-1} + 5 \ln|2x - 1| + c$$

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13 - Answers

https://www.madasmaths.com/archive/iygb_practice_papers/c2_practice_papers/c2_v_solutions.pdf

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14 - Answers

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