A manufacturer of tennis balls has a daily cost $C(x) = 200 - 10x + 0.01x^2$ where C is the total cost in £ and x is the number of tennis balls produced.

(a) Write C in the form $-A + B(x - C)^2$ where A, B, C are constants to be found

(b) What number of tennis balls produces the minimum cost?

2

A cubic polynomial is defined as

$$p(x) = x^3 - 4x^2 + x + 6$$

(a) Fully factorise the cubic

(b) Sketch the cubic

TAP FOR ANSWERS

3

$$f(x) = \frac{5x^2 + 7x}{2x^4}$$

(a) Split f(x) into two fractions and find an expression for f'(x)

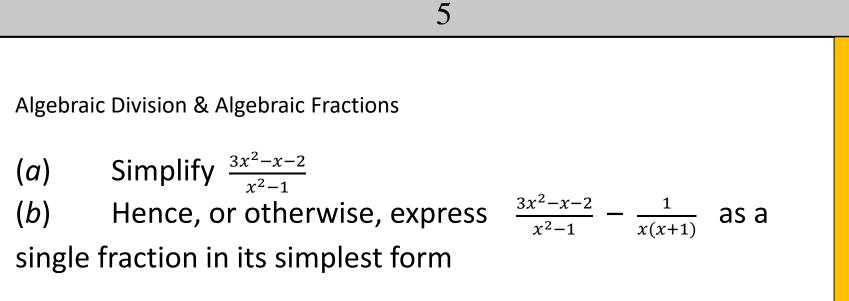
(b) Now consider the functions $g(x) = 5x^2 + 7x$ and $h(x) = 2x^4$. Find expressions for g'(x) and h'(x)

(c) Now,
$$f(x) = \frac{g(x)}{h(x)}$$
 Which one of the following rules is true?
A $f(x) = \frac{g'(x)}{h'(x)}$
B $f(x) = \frac{g'(x)h(x)+g(x)h'(x)}{h(x)}$
C $f(x) = \frac{g'(x)h(x)-g(x)h'(x)}{h(x)^2}$
D $f(x) = \frac{g'(x)h(x)+g(x)h'(x)}{h(x)^2}$
E $f(x) = \frac{g(x)h'(x)-g'(x)h(x)}{h(x)}$

4

The circle *C* has equation $x^2 + y^2 - 12x + 8y + 16 = 0$

- (a) Find the centre and radius of *C*
- (b) Given that *C* crosses the *x* axis at the points *A* and *B*, find the length *AB* giving your answer in the form $k\sqrt{5}$



TAP FOR ANSWERS

6

A large tank is in the shape of a cuboid with a rectangular base and no top. Two of the vertical opposite faces of the cuboid are square and the height of the cuboid is x metres.

(a) given that the surface area of the tank is 54 m^2 , show that the capacity, V, of the tank is given by $V = 18x - \frac{2}{3}x^3$.

(b) Find the maximum value for V, fully justifying the fact that it is the maximum value.

7

Solve these equations for $0 \le \theta \le 360^\circ$, giving θ to 1 decimal place where appropriate:

(a) $\sin(\theta + 15^\circ) = 3\cos(\theta + 15^\circ)$

(b) $\sin\theta\cos\theta = \frac{1}{2}$

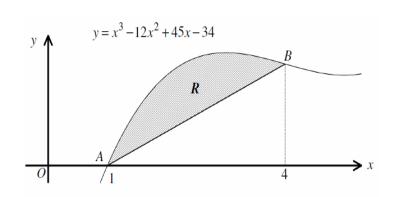
8

The circle *C* has equation $x^2 - 2kx + y^2 - ky + 15 = 0$. The line *l* passes through the point *P* (5, 9), has gradient 2, and is a tangent to the circle *C*.

Find the value of *k*, where k is a positive constant

9

TAP FOR ANSWERS



The figure above shows the curve with equation

$$y = x^3 - 12x^2 + 45x - 34$$

The points *A* and *B* lie on the curve, where x = 1 and x = 4 respectively. The finite region *R* is bounded by the curve and the straight line segment *AB*. Show that the area of *R*, shown shaded in the figure is $\frac{81}{4}$

10

Prove that every integer that is a perfect cube is a multiple of 9 or is one more than a multiple of 9 or is one less than a multiple of 9.

11

Use your knowledge of the approximations for *cosx* and *sinx*, to find the value of

(a) $\frac{\cos 3x - 1}{x^2}$ (b) $\frac{\cos 3x - 1}{x \sin 4x}$ (c) $\frac{4x \sin 2x}{x^2}$

for small values of *x*.

12

Prove the following identities:

- (a) $\tan^2 x + \cot^2 x \equiv \sec^2 x + \csc^2 x 2$
- (b) $(\sec^2 x + \tan^2 x)(\csc^2 x + \cot^2 x) \equiv 1 + 2 \sec^2 x \csc^2 x$

13 By using the chain rule find $\frac{dy}{dx}$ (c) $y = \sqrt{4x + 2x^2}$ (a) $y = (4x^2 - 3)^5$ (b) $y = \frac{1}{(7-2x^3)}$ TAP FOR ANSWERS (e) $y = sin^2 x$ (f) $y = \sin(x^2)$ (d) $y = \sin 3x$ (g) $y = \cos^2 3x$

14

1. By using the product rule find $\frac{dy}{dx}$ simplifying your answers

(a)
$$y = x^4 (x^5 - 2)^6$$
 (b) $y = x^2 \sin x$ (c) $y = \sqrt{x} \cos 3x$

2. By using the quotient rule find the derivatives of the following:

(a)
$$\frac{x+3}{2x+1}$$
 (b) $\frac{3x^2}{(2x-1)^2}$ (c) $\frac{x^4}{\cos 3x}$



1. Complete this old spec paper

2.

https://www.madasmaths.com/archive/iygb_practice_papers/c1_practice_papers/c1_n.pdf

TAP FOR ANSWERS

1 - Answers

(a) A = 2300, B = 0.01, C = 500

(b) 500

2 - Answers

(x-3)(x-2)(x+1)

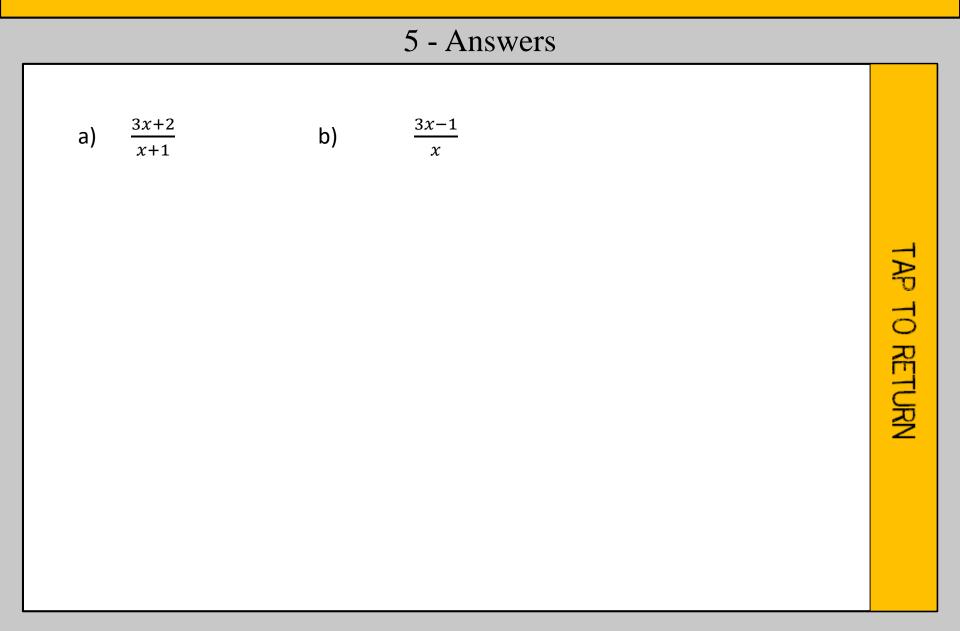
3 - Answers

(a) $-\frac{5}{x^3} - \frac{21}{2x^4}$
(b) 10x + 7, 8x ³
(c) C

4 - Answers

(a) Centre (6, -4) radius 6

(b) k = 4





7 - Answers

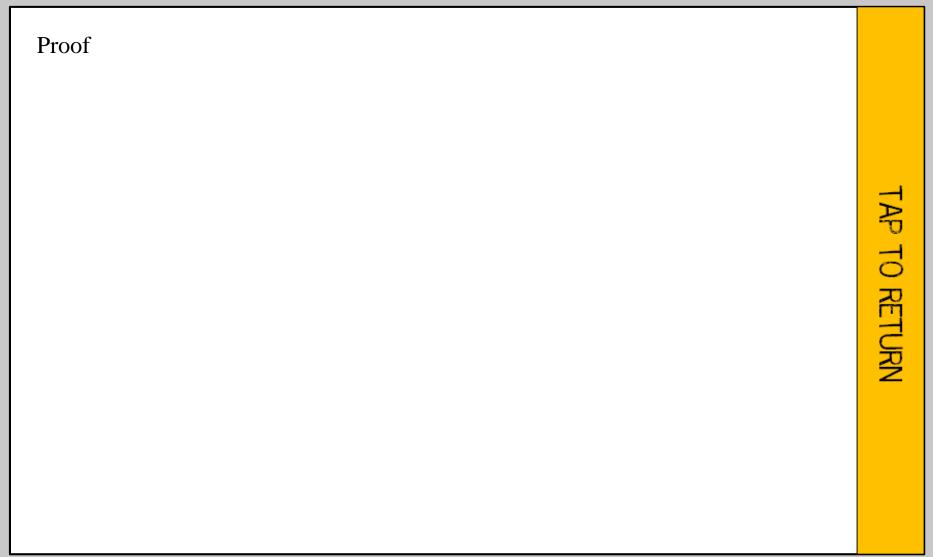
(a) 56.6°, 236.6°

(b) 45°, 225°



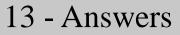
9 - Answers

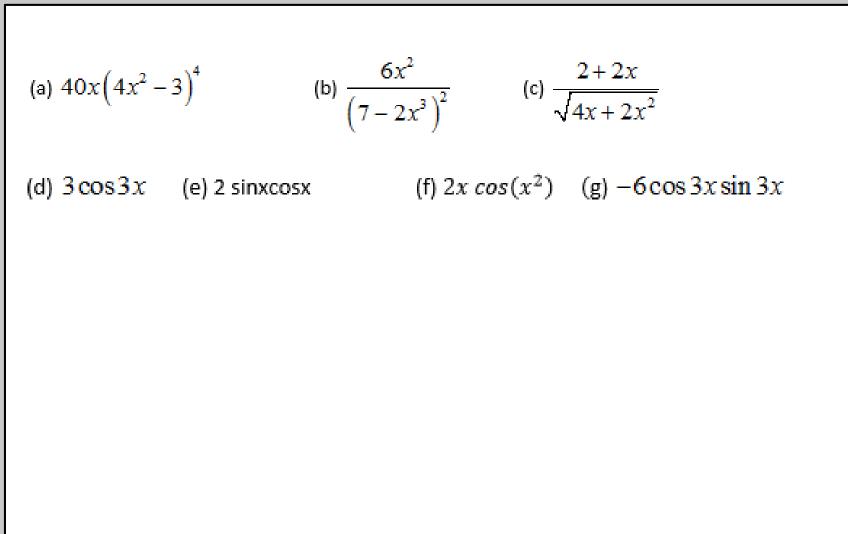
Proof











14 - Answers

1. (a) $2x^{3}(x^{5}-2)^{5}(17x^{5}-4)$ (b) $x^{2}\cos x + 2x\sin x$ (c) $-3\sqrt{x}\sin 3x + \frac{\cos 3x}{2\sqrt{x}}$

2. (a)
$$\frac{-5}{(2x+1)^2}$$
 (b) $\frac{-6x}{(2x-1)^8}$ (c) $\frac{x^3(3xsin3x+4\cos 3x)}{\cos^2 x}$

15 - Answers

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2.

1.