Without using your calculator, find the exact value of:

```
(a) \sin 30^{\circ} \cos 60^{\circ} + \cos 30^{\circ} \sin 60^{\circ}
```

```
(b) \sin 33^{\circ} \cos 27^{\circ} + \cos 33^{\circ} \sin 27^{\circ}
```

```
(c) \frac{\tan 45^\circ + \tan 15^\circ}{1 - \tan 45^\circ \tan 15^\circ}
```

(d) 
$$\frac{\tan\frac{7\pi}{12} - \tan\frac{\pi}{3}}{1 + \tan\frac{7\pi}{12}\tan\frac{\pi}{3}}$$

(e)  $\sqrt{3}\cos 15^\circ - \sin 15^\circ$ 

2

Express the following as a single sine, cosine or tangent:

```
(a) \sin 15^{\circ} \cos 20^{\circ} + \cos 15^{\circ} \sin 20^{\circ}
```

```
(b) \sin 58^\circ \cos 23^\circ - \cos 58^\circ \sin 23^\circ
```

 $(c) \frac{\tan 76^\circ - \tan 45^\circ}{1 + \tan 76^\circ \tan 45^\circ}$ 

(d) 
$$\sin \frac{1}{2}\theta \cos 2\frac{1}{2}\theta + \cos \frac{1}{2}\theta \sin 2\frac{1}{2}\theta$$

(e)  $\frac{\tan 2\theta + \tan 3\theta}{1 - \tan 2\theta \tan 3\theta}$ 

3

(a) Find the value of x for which the curve  $y = 800x + \frac{2}{x}$ , x > 0, has a stationary point.

(b) Using the second derivative, determine whether this point is a local maximum or minimum point.

4

The circle *C* has centre (5, 2) and passes through the point (7, 3).

(a) Find an equation for C
(b) Show that the line y = 2x - 3 is tangent to C and find the coordinates of the point of contact

HINT: Show equal roots

5

Solve the following equation on the interval  $0 \le \theta \le 2\pi$ . Give answers to 3 decimal places.

$$\frac{4}{\sec^2 x} + 3\cos x = 2\cot x \tan x$$

#### 6

Prove that 
$$\cos \theta + \cos \left(\theta + \frac{2\pi}{3}\right) + \cos \left(\theta + \frac{4\pi}{3} = 0\right)$$

You must show each stage of your working.

7

Given that  $\sin x(\cos y + 2 \sin y) = \cos x(2 \cos y - \sin y)$ , find the value of  $\tan(x + y)$ 

#### 8

Split the following into partial fractions:

a) 
$$\frac{3x^2 - 2x + 1}{2x^4 + x}$$
  
b)  $\frac{4x^3 - 12x^2 - 22x - 3}{2x^4 + x^2}$ 

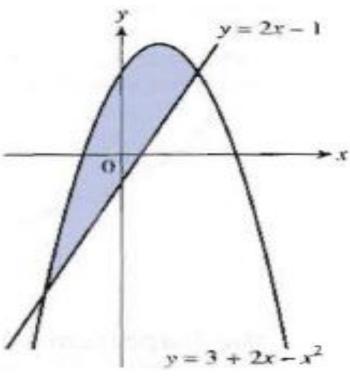
 $7x - 2x^2 + 4$ 

#### 9

Show that  $\frac{4x^3-6x^2+8x-5}{2x+1}$  can be written in the form  $Ax^2 + Bx + C + \frac{D}{2x+1}$  where *A*, *B*, *C* and *D* are constants to be found.

#### 10

Find the area shaded between the line y = 2x - 1 and the curve  $y = 3 + 2x - x^2$ 



#### 11

(a) Sketch the graph of y = <sup>3</sup>/<sub>x</sub>, remembering to include the equations of any asymptotes. Add to this sketch, the line y = a - 3x which is a tangent to the curve y = <sup>3</sup>/<sub>x</sub> at the point *A*, and the line y = b - 3x which is tangent to the curve y = <sup>3</sup>/<sub>x</sub> and the point *B*.
(b) Find the values of *a* and *b*

12

Use differentiation from first principles to prove that:

if  $f(x) = 3x^2$ , f'(x) = 6x.

13

The point (6, 1) lies on the circle  $x^2 + y^2 - 8x - 4y + 15 = 0$ .

(a) Find the equation of the normal to the circle at this point

(b) Find the coordinates of the second point at which the normal cuts the circle

#### 14

Disproof by Counter Example

E.g. Show that the statement " $n^2 - n + 1$  is a prime number for all values of n" is untrue. Ans. n=5 since  $5^2 - 5 + 1 = 21$  and 21 is not a prime number.

Therefore, the statement is untrue.

a) Prove by counter-example that the product of an odd and even number is never a perfect square.

15

Complete this old spec paper,

https://www.madasmaths.com/archive/iygb\_practice\_papers /c1\_practice\_papers/c1\_m.pdf

Exclude qs 3 and 7

#### 1 - Answers



#### 2-Answers

TAP TO RETURN

(a) sin 35°
(b) sin 35°
(c) tan 31°
(d) sin 3 <i>θ</i>

(e)  $\tan 5\theta$ 

3 - Answers

(a)  $\pm \frac{1}{20}$ (b)  $x = \frac{1}{20}$  Minimum (you need to give a reason)  $x = -\frac{1}{20}$  Maximum

TAP TO RETURN

4 - Answers

(a) 
$$(x-5)^2 + (y-2)^2 = 5$$
  
(b) (3, 3)

#### 5 - Answers

1.131, 5.152

6 - Answers

Write 
$$\theta$$
 as  $\left(\theta + \frac{2\pi}{3}\right) - \frac{2\pi}{3}$  and  $\theta + \frac{4\pi}{3}$  as  $\left(\theta + \frac{2\pi}{3}\right) + \frac{2\pi}{3}$ 

Use the addition formulae for cos and simplify.

TAP TO RETURN

#### 7 - Answers



#### 8 - Answers

(a) 
$$\frac{1}{x} + \frac{-2x^2 + 3x - 2}{2x^3 + 1}$$
  
(b)  $-2x - 1 - \frac{3}{4 - x} + \frac{1}{2x + 1}$ 

TAP TO RETURN

9 - Answers

A = 2, B = -4, C = 6, D = -11

#### 10 - Answers



#### 11 - Answers

(a) Use desmos

(b) 6 and - 6

#### 12 - Answers



#### 13 - Answers

(a) x + 2y - 8 = 0(b) (2, 3)

#### 14 - Answers

Even number 4 Odd number 9 4x9=36

Since 36 is a perfect square, an even number times an odd number can equal a perfect square, therefore the statement is untrue. TAP TO RETURN

15 - Answers

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