

1. a) CORRECT METHOD ELIMINATION OR COMPARISON OF COEFFICIENTS

E.g. $2x^3 - 3 \equiv A(x-1)^2 + B(x-1) + C$ OR SIMILAR M1

$A=2 \quad B=4 \quad C=-1$ A3

b) $2x + 4\ln|x-1| + (x-1)^{-1}$ M3 ft the coefficients only from (a)

(.....) - (.....) ATTEMPTED CORRECTLY. M1 ft.

$\frac{3}{2} + 4\ln 2$ OR $\frac{3}{2} + \ln 16$ c.a.o. A1

2. a) USES GAP OF 0.25 (MAY BE INPUT FROM THEIR y VALUES) B1

1, 0.9394, 0.7788, 0.5998, 0.3679
(ALLOW ONE ERROR OR OMISSION) MA1

$\frac{0.25}{2} \left[\text{"FIRST"} + \text{"LAST"} + 2 \times \text{"SUM OF REST"} \right]$ M1

A.W.R.T 0.743

(ALLOW 0.74 WITH WORKING) A1

b) STATE OF $e^{-x^2} \times e^3$ M1

$e^3 \times \text{"THAT 0.743"}$ OR A.W.R.T 14.9 MA1

3. a)

SIGHT OF $3x^2$

B1

$$\frac{dx}{dt} \times \frac{dv}{dt} \text{ o.e. or } \frac{1}{3x^2} \times 0.108 \text{ or } \frac{9}{250x^2} \quad M1$$

$$\frac{9}{250 \times 3^2} \text{ or SUBS } x=3 \text{ INTO "THAT"} \frac{dx}{dt} \text{ SO LONG AS } \frac{dx}{dt} = f(x) \quad M1 \text{ ft}$$

$$0.04 \text{ or } \frac{1}{250} \quad A1 \text{ c.a.o.}$$

b)

SIGHT OF $12x$

B1

$$12x \times \frac{9}{250x^2} \text{ or } 12x \times "0.004" \quad M1 \text{ ft.}$$

$$0.144 \text{ o.e. f.g. } \frac{18}{125} \quad A1 \text{ c.a.o.}$$

4.

$$12x^2$$

$$\pm 6y \pm 6x \frac{dy}{dx}$$

(ALLOW SIM ERRORS)

$$+ 3^y \ln 3 \times \frac{dy}{dy}$$

M3

$$\frac{dy}{dx} = \frac{12x^2 - 6y}{6x - 3^y \ln 3} \quad \text{OR} \quad 12x^2 - 6y - 6x \frac{dy}{dx} + 3^y \ln 3 \frac{dy}{dx} = 0 \quad A1$$

SUBS $x=2, y=3$ INTO THAT "dy/dx":(MAY BE AN UNSIMPLIFIED EXPRESSION OF $\frac{dy}{dx}$)) M1

$$\frac{10}{4 - 9 \ln 3} \text{ OBTAINED CORRECTLY OR } k=10 \quad A1$$

5.

$$-5 = \frac{a}{t} - 1 \quad \text{B1}$$

$$3 = \frac{t+a}{t+1} \quad \text{B1}$$

SOLVES SIMULTANEOUSLY, BY AT LEAST ONE NON TRIVIAL STEPS TO FIND a OR t M1

$$t = -\frac{1}{2} \quad \text{A1}$$

$$a = 2 \quad \text{A1}$$

ATTEMPTS TO ELIMINATE t FROM PARAMETRICS WITHOUT a M1

CORRECTLY ARRIVES TO THE ANSWER ON TN $y = \frac{2x+4}{x+3}$ MA1

6.

$$x^2 \frac{dy}{dx} = y(x+1) \quad \text{B1}$$

$$\frac{1}{y} dy = \frac{x+1}{x^2} dx \quad \text{OR} \quad \frac{1}{y} dy = \int \frac{1}{x} + \frac{1}{x^2} \quad \text{M1}$$

INTEGRALS ~~SPEN~~ ON BOTH SIDES OF THIS $\int f(y) dy = \int f(x) dx$ M1 ft.

$$\ln y = \ln x - \frac{1}{x} + C \quad \text{o.e.} \quad \text{A3 -1 eeo}$$

$$y = e^{\ln x - \frac{1}{x} + C} \quad \text{MA1}$$

$$y = Ax e^{-\frac{1}{x}} \quad (\text{MAY USE ANY SENSIBLE LETTER INSTEAD OF A}) \quad \text{A1 c.a.o}$$

7. a) $1 + 2\cos 2x + \cos^2 2x$ B1

START OF $\frac{1}{2} + \frac{1}{2}\cos 4x$ OR $\cos 4x = 2\cos^2 2x - 1$ M1
 OR $\frac{1}{2} + \frac{1}{2}\cos 2x$ OR $\cos 2x = 2\cos^2 x - 1$

$1 + 2\cos 2x + (\frac{1}{2} + \frac{1}{2}\cos 4x)$ START DEPENDENT ON ANY OF THESE BEFORE ARRIVING AT THE ANSWER GIVEN

A1

b) $\pi \int_0^{\frac{\pi}{2}} (1 + \cos 2x)^2 dx$ OR $\pi \int_0^{\frac{\pi}{2}} \frac{3}{2} + 2\cos 2x + \frac{1}{2}\cos 4x$ B1

$\frac{3}{2}x + \sin 2x + \frac{1}{8}\sin 4x$ -A3

(.....) - (.....) f.g. $(\frac{3\pi}{4} + 0 + 0) - (0)$
 OR $\frac{3\pi}{4} - 0$

BEFORE CORRECTLY ARRIVING AT THE ANSWER GIVEN $\frac{3}{4}\pi^2$ MA1

8. a) $2\lambda + 10 = 6$ M1
 $a=7$ $b=5$ A1 A1

b) $y + 2z = 0$ M1

$x=7, y=1+5, z=2\lambda+10$

(ALL 3 SEEN, MAY APPEAR IN PART a) M1

$(\lambda+5) + 2(2\lambda+10) = 0$ M1

$\lambda = -5$ A1

$Q(7, 0, 0)$ A1

c) $3 = 2$ B1 c.a.o

9. a) $1 - 3kx + 6k^2x^2 - 10k^3x^3$ M1 A3

(ONE METHOD MARK FOR AN UNSIMPLIFIED EXPANSION)
 (ONE SMALL ERROR IS OK)

b) ATTEMPTS POLYNOMIAL MULTIPLICATION BETWEEN
 $(6-x)$ AND THEIR EXPANSION M1

SIGHT OF $3kx^2$ M1

SIGHT OF $3k^2x^2$ OR $36k^2$ M1

$36k^2 + 3k - 3 = 0$ O.E. f.g. $12k^2 + k - 1 = 0$ M1

$(3k+1)(4k-1)$ M1

$k = \left\langle \begin{matrix} 1/4 \\ -1/3 \end{matrix} \right. (BOTH) A1$

10.

$-2x \cos 3x - \int -2 \cos 3x$ O.E.
 $\pm \frac{2}{3} \sin 3x$ M1 dgp

M1 STRUCTURE OF PART II
 M1 M1 EACH "LUMP"

$\frac{2\pi}{3}$ C.a.o. A1