

Paper Reference(s)

**6665/01**

**Edexcel GCE**

**Core Mathematics C3**

**Advanced Level**

**Thursday 16 June 2011 – Afternoon**

**Time: 1 hour 30 minutes**

**Materials required for examination**

Mathematical Formulae (Pink)

**Items included with question papers**

Nil

**Calculators may NOT be used in this examination.**

**Instructions to Candidates**

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Write the name of the examining body (Edexcel), your centre number, candidate number, the unit title (Core Mathematics C3), the paper reference (6665), your surname, initials and signature.

**Information for Candidates**

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A booklet 'Mathematical Formulae and Statistical Tables' is provided.  
Full marks may be obtained for answers to ALL questions.  
There are 8 questions in this question paper. The total mark for this paper is 75.

**Advice to Candidates**

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You must ensure that your answers to parts of questions are clearly labelled.  
You must show sufficient working to make your methods clear to the Examiner.  
Answers without working may not gain full credit.

1. Differentiate with respect to  $x$

(a)  $\ln(x^2 + 3x + 5)$ , (2)

(b)  $\frac{\cos x}{x^2}$ . (3)

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2.  $f(x) = 2 \sin(x^2) + x - 2, \quad 0 \leq x < 2\pi.$

(a) Show that  $f(x) = 0$  has a root  $\alpha$  between  $x = 0.75$  and  $x = 0.85$ . (2)

The equation  $f(x) = 0$  can be written as  $x = [\arcsin(1 - 0.5x)]^{\frac{1}{2}}$ .

(b) Use the iterative formula

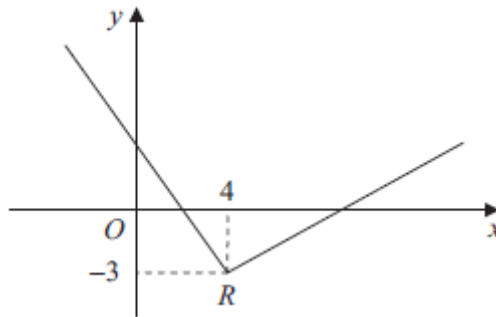
$$x_{n+1} = [\arcsin(1 - 0.5x_n)]^{\frac{1}{2}}, \quad x_0 = 0.8,$$

to find the values of  $x_1$ ,  $x_2$  and  $x_3$ , giving your answers to 5 decimal places. (3)

(c) Show that  $\alpha = 0.80157$  is correct to 5 decimal places. (3)

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3.



**Figure 1**

Figure 1 shows part of the graph of  $y = f(x)$ ,  $x \in \mathbb{R}$ .

The graph consists of two line segments that meet at the point  $R(4, -3)$ , as shown in Figure 1.

Sketch, on separate diagrams, the graphs of

(a)  $y = 2f(x + 4)$ , (3)

(b)  $y = |f(-x)|$ . (3)

On each diagram, show the coordinates of the point corresponding to  $R$ .

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4. The function  $f$  is defined by

$$f: x \mapsto 4 - \ln(x + 2), \quad x \in \mathbb{R}, \quad x \geq -1.$$

(a) Find  $f^{-1}(x)$ . (3)

(b) Find the domain of  $f^{-1}$ . (1)

The function  $g$  is defined by

$$g: x \mapsto e^{x^2} - 2, \quad x \in \mathbb{R}.$$

(c) Find  $fg(x)$ , giving your answer in its simplest form. (3)

(d) Find the range of  $fg$ . (1)

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5. The mass,  $m$  grams, of a leaf  $t$  days after it has been picked from a tree is given by

$$m = pe^{-kt},$$

where  $k$  and  $p$  are positive constants.

When the leaf is picked from the tree, its mass is 7.5 grams and 4 days later its mass is 2.5 grams.

- (a) Write down the value of  $p$ . (1)

- (b) Show that  $k = \frac{1}{4} \ln 3$ . (4)

- (c) Find the value of  $t$  when  $\frac{dm}{dt} = -0.6 \ln 3$ . (6)
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6. (a) Prove that

$$\frac{1}{\sin 2\theta} - \frac{\cos 2\theta}{\sin 2\theta} = \tan \theta, \quad \theta \neq 90n^\circ, \quad n \in \mathbb{Z}. \quad (4)$$

- (b) Hence, or otherwise,

- (i) show that  $\tan 15^\circ = 2 - \sqrt{3}$ , (3)

- (ii) solve, for  $0 < x < 360^\circ$ ,

$$\operatorname{cosec} 4x - \cot 4x = 1. \quad (5)$$

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7. 
$$f(x) = \frac{4x-5}{(2x+1)(x-3)} - \frac{2x}{x^2-9}, \quad x \neq \pm 3, \quad x \neq -\frac{1}{2}.$$

(a) Show that

$$f(x) = \frac{5}{(2x+1)(x-3)}.$$

**(5)**

The curve  $C$  has equation  $y = f(x)$ . The point  $P \left( -1, -\frac{5}{2} \right)$  lies on  $C$ .

(b) Find an equation of the normal to  $C$  at  $P$ .

**(8)**

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8. (a) Express  $2 \cos 3x - 3 \sin 3x$  in the form  $R \cos (3x + \alpha)$ , where  $R$  and  $\alpha$  are constants,  $R > 0$  and  $0 < \alpha < \frac{\pi}{2}$ . Give your answers to 3 significant figures.

**(4)**

$$f(x) = e^{2x} \cos 3x.$$

(b) Show that  $f'(x)$  can be written in the form

$$f'(x) = Re^{2x} \cos (3x + \alpha),$$

where  $R$  and  $\alpha$  are the constants found in part (a).

**(5)**

(c) Hence, or otherwise, find the smallest positive value of  $x$  for which the curve with equation  $y = f(x)$  has a turning point.

**(3)**

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**TOTAL FOR PAPER: 75 MARKS**

**END**